

Find the derivative of each quantity.

Note that u and v are functions of x (i.e. $u(x)$, $v(x)$)

1) $\frac{d}{dx} (\sin u) = \cos u \cdot u'$

2) $\frac{d}{dx} (\sec u) = \sec u \tan u \cdot u'$

3) $\frac{d}{dx} (\ln |u|) = \frac{1}{u} \cdot u'$

4) $\frac{d}{dx} (\cos u) = -\sin u \cdot u'$

5) $\frac{d}{dx} (\tan^{-1} u) = \frac{1}{1+u^2} \cdot u'$

6) $\frac{d}{dx} (\csc u) = -\csc u \cot u \cdot u'$

7) $\frac{d}{dx} (\sin^{-1} u) = \frac{1}{\sqrt{1-u^2}} \cdot u'$

8) $\frac{d}{dx} (\cot u) = -\csc^2 u \cdot u'$

9) $\frac{d}{dx} (e^u) = e^u \cdot u'$

10) $\frac{d}{dx} (\sec^{-1} u) = \frac{1}{u\sqrt{u^2-1}} \cdot u'$

11) $\frac{d}{dx} (\tan u) = \sec^2 u \cdot u'$

12) $\frac{d}{dx} (a) = 0$

where $a = \text{constant}$

13) $\frac{d}{dx} (\cos^{-1} u) = \frac{-1}{\sqrt{1-u^2}} \cdot u'$

14) $\frac{d}{dx} (uv) = u'v + uv'$

15) $\frac{d}{dx} \left(\frac{u+v}{u-v} \right) = \frac{u'v + uv' + v'v - uv'}{v^2 - uv'}$

16) $\frac{d}{dx} \left(\frac{u}{v} \right) = \frac{v^2}{v^2}$

17) $\frac{d}{dx} (f(g(x))) = f'(g(x)) \cdot g'(x)$

18) $\frac{d}{dx} (u^n) = n u^{n-1} \cdot \frac{du}{dx}$

where n is an integer

19) $\frac{d}{dx} (a^u) = a^u \ln a \cdot u'$

20) $\frac{d}{dx} (\log_a |u|) = \frac{1}{u \cdot \ln a} \cdot u'$

$$\log_a |u| = \frac{\ln |u|}{\ln a}$$

Integrate as indicated. Note that a is a positive real number.

21) $\int \cos(u) du = \sin u + C$

22) $\int \frac{1}{u} du = \ln |u| + C$

23) $\int \sec(u) du = \ln |\sec u + \tan u| + C$

24) $\int \sin(u) du = -\cos u + C$

25) $\int e^u du = e^u + C$

26) $\int \sec^2 u du = \tan u + C$

27) $\int a^u du = \frac{a^u}{\ln a} + C$

28) $\int \csc^2 u du = -\cot u + C$

29) $\int \sec u \tan u du = \sec u + C$

30) $\int \tan u du = \ln |\sec u| + C$

31) $\int \csc u du = \ln |\csc u + \cot u| + C$

32) $\int \frac{1}{\sqrt{1-u^2}} du = \sin^{-1} u + C$

33) $\int \frac{1}{1+u^2} du = \tan^{-1} u + C$

34) $\int \csc u \cot u du = -\csc u + C$

35) $\int \frac{1}{u\sqrt{u^2-1}} du = \sec^{-1} u + C$

36) $\int \cot u du = \ln |\csc u| + C$